

MATH 152 98-2 Solutions for Assignment 1

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2. $f(x) = 3x - 1$; the partition P of $[-2, 2]$ is $\{-2, -1.2, -0.6, 0, 0.8, 1.6, 2\}$.
 x_i^* is the midpoint of the i^{th} interval.

(a) $\|P\| = \text{Max}(0.8, 0.6, 0.6, 0.8, 0.8, 0.4) = 0.8$.

(b) The Riemann sum associated with this partition and this choice of $\{x_i^*\}$ is

$$\sum_{i=1}^n f(x_i^*) \Delta x_i = f(-1.6) \cdot 0.8 + f(-0.9) \cdot 0.6 + f(-0.3) \cdot 0.6 + f(0.4) \cdot 0.8 + f(1.2) \cdot 0.8 + f(1.8) \cdot 0.4 = \\ = -5.8 \cdot 0.8 - 3.7 \cdot 0.6 - 1.9 \cdot 0.6 + 0.2 \cdot 0.8 + 2.6 \cdot 0.8 + 4.4 \cdot 0.4 = -4.$$

4. $f(x) = x + x^2$; the partition P of $[-2, 0]$ is given by $\{-2, -1.5, -1, -0.7, -0.4, 0\}$.
 x_i^* is the left endpoint of the i^{th} interval.

(a) $\|P\| = \text{Max}(0.5, 0.5, 0.3, 0.3, 0.4) = 0.5$.

(b) The Riemann sum associated with this partition and this choice of $\{x_i^*\}$ is

$$\sum_{i=1}^n f(x_i^*) \Delta x_i = f(-2) \cdot 0.5 + f(-1.5) \cdot 0.5 + f(-1) \cdot 0.3 + f(-0.7) \cdot 0.3 + f(-0.4) \cdot 0.4 = \\ = 2 \cdot 0.5 + 0.75 \cdot 0.5 + 0 \cdot 0.3 - 0.21 \cdot 0.3 - 0.24 \cdot 0.4 = 1.216.$$

$$16. \int_{-2}^7 (6 - 2x) dx = \lim_{n \rightarrow \infty} \frac{9}{n} \sum_{i=1}^n f(-2 + (9i)/n) = \lim_{n \rightarrow \infty} \frac{9}{n} \sum_{i=1}^n \left[10 - \frac{18i}{n} \right] = \\ = \lim_{n \rightarrow \infty} \frac{9}{n} \left[10n - \frac{18}{n} \cdot \frac{n(n+1)}{2} \right] = \lim_{n \rightarrow \infty} \left[90 - 81 \left[1 + \frac{1}{n} \right] \right] = 9.$$

30. $\lim_{\|P\| \rightarrow 0} \sum_{i=1}^n \sqrt{x_i} \Delta x_i = \int_1^4 \sqrt{x} dx$ if the partition P is on the interval $[1, 4]$.

34. $\lim_{n \rightarrow \infty} \frac{1}{n} \sum_{i=1}^n \frac{1}{1 + (i/n)^2} = \int_0^1 \frac{dx}{1 + x^2}$.

There are other correct answers.

36. $\int_1^1 x^2 \cos x dx = 0$.

See Note 6 on Page 338 of the text.

40. $\int_3^6 (4 - 7x) dx = \int_3^6 4 dx - 7 \int_3^6 x dx = 4(6 - 3) - 7 \cdot \frac{1}{2} (6^2 - 3^2) = -82.5$.